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A Procedure for Automated Gas Turbine Blade Fault Identification Based on Spectral Pattern Analysis

A method for diagnosing the existence and the kinds of faults in blades of a gas turbine compressor is presented in the present paper. The innovative feature of this method is that it performs the diagnosis automatically, that is, it gives a direct answer to whether a fault exists and what type of fault it is, without requiring the interpretation of results by a human expert. This is achieved by derivation of the values of discriminants calculated from spectral patterns of fast response measurement data. A decision about the corresponding engine status is then derived according to the values of the discriminants. In the paper, the procedure of examining the suitability of particular parameter discriminants and the constitution of a related knowledge base is described. The derivation of decisions by a computer, and on what engine condition a particular measurement data set corresponds, are then described.

1 Introduction

Development of effective gas turbine condition monitoring and fault diagnosis methods has been the target of considerable research in recent years. Whether the methods are of the gas path analysis type or based on dynamic data, such as vibrations, the aim is to take advantage of the capabilities of modern computers in order to provide a fast and reliable answer to what the condition of the engine is when measurements are available. The introduction of expert systems, in particular, has provided the possibility of integrating the data processing and decision making techniques into computerized procedures, which can provide information of direct use even to the inexperienced user.

The existence of mechanical faults can be revealed by vibration monitoring techniques, which cover a wide range of faults, as, for example, discussed by Lifson et al. (1990). On the other hand, the possibility of detecting even minor faults of individual blades has been demonstrated by Mathiouidakis et al. (1991). Derivation of the decision about the existence of a fault is based on the calculation of some characteristic quantities and the user's judgment, according to the observed features and existing experience.

The methodology proposed in the present paper gives the possibility of extracting a decision about the existence of a fault by a digital computer, eliminating the need for interpretation of the results by specialized personnel. The extraction of such a decision is possible by application of pattern recognition methods. Such methods have been applied in various

other domains, e.g., monitoring of bearing elements (e.g., Li and Wu, 1989), machine tools (Emel and Kannatey-Asihm, 1989), gearboxes (Barschdorff et al., 1987). Applications to turbomachinery faults related to dynamic data have first been proposed by Barschdorff (1986). The work presented there was based on features of time traces from casing accelerometers.

The work we present here is based on spectral features of measurements of various dynamic quantities, such as internal pressure, casing acceleration, and acoustic data. Its particular feature is that before applying the pattern recognition technique, the data are preprocessed in order to derive fault signatures. On the other hand, the test case analyzed consists of a commercial industrial gas turbine operating at different loads, representing thus a realistic industrial test case of application.

The way the method is organized allows its direct inclusion in an expert system. In particular, it replies to the need of obtaining computer tools for the diagnosis of specific engine problems, as identified by Doel (1990).

2 Experimental Data

The present investigation was based upon measurements on an industrial gas turbine into which different faults were introduced. The test engine was the Ruston Tornado, described by Carchedi and Wood (1982). The instrumentation layout and measurement conditions are described by Loukis et al. (1991). For completeness, we repeat here the instruments used and the examined faults.

During the experimental campaign four categories of measurement were performed simultaneously:

- (a) Unsteady internal wall pressure, instruments PT1 to PT5. PT2 faces rotor 1, PT3 rotor 2, etc.

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(b) Casing vibration, with accelerometers mounted at the outside compressor casting (instruments ACT 1 to ACT 6).
 (c) Shaft displacement at compressor bearings, with a Bendix Nevada system.
 (d) Sound pressure levels, with double layer microphones.

Five experiments were performed testing the datum healthy engine and engines with the following four faults:
Fault 1. Rotor fouling: All stage 2 rotor blades were coated with textured paint in order to roughen blade surface and alter their contour, in order to simulate a fault of all the blades of a rotor.
Fault 2. Individual rotor blade fault: Two blades of stage 1, intact, were coated by textured paint in order to simulate a slight individual rotor blade fault.
Fault 3. Individual rotor blade twisted: A single blade of stage 1 rotor was twisted in order to simulate a severe rotor blade fault.
Fault 4. Station blade restaggering: two stage 1 stator blades were misaligned in order to simulate a minor fault.

Tests were performed at four different engine loads: full load, half load, quarter load, and no load (termed operating point A, B, C, D, respectively, hereafter), with the intact engine as well as the faulty engines. This means that for each fault we obtain four data sets, one at each load.

3 Spectral Difference Pattern Analysis

In order to develop an automated fault identification method, it is necessary to derive some quantitative characteristics of the measured signals, reflecting the presence of faults. The derivatives have been demonstrated by Matikoudakis et al. (1991).

This technique is used as a departing point for the methodology presented in this paper. Using this procedure, we examine not only fast response pressure measurements, but all the different hydrodynamic measurements mentioned in the previous section. A difference pattern (fault index) is derived from the following expression:

$$\mu(U) = 20[\log(\delta p(U)) - \log(\delta p_h(U))] \quad (1)$$

$\mu(U)$ is the fault index, which is thus a set of values in function of frequency, $\delta p(U)$ is the power spectrum of the signal of the measuring instrument from a faulty engine, $\delta p_h(U)$ is the same spectrum from a healthy engine. It is useful to remember that expression (1) was selected among several algebraic combinations of spectra of pressure measurements, by Matikoudakis et al. (1991), on the basis of two observations: This index measures scalar functions characteristic of the fault index, and (ii) to distinguishable forms for each fault.

The purpose of the fault index analysis we present now is: (i) to improve diagnostic capabilities by selecting only the most relevant information contained in indices, (ii) to derive some scalar functions characteristic of the fault index, and (iii) to specify an indication of the differentiation of the readings of a specific instrument by a fault is the amplitude of the corresponding reduced pattern (the "amplitude" we mean the range between the minimum and maximum values of the pattern). If the reduced pattern of a fault is of higher amplitude than that of another fault, this means that the transducer is more sensitive to the first fault than to the second.

On the other hand, in order to be suitable as fault signatures, the reduced patterns have to exhibit two basic features:

(a) Reduced patterns corresponding to one fault should be similar, when different experiments with this fault are considered.

(b) Reduced patterns of two different faults should be dissimilar in order to be distinguishable.

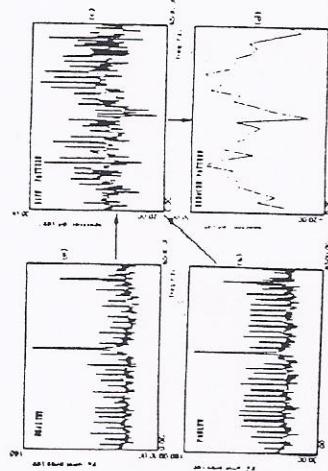


Fig. 1 Power spectra of unsteady pressure transducer 2 (P2) with the corresponding fault index and the reduced pattern

This is done by a filter of unit gain at the rotational harmonics and zero at the other frequencies, defined by the following equation:

$$h(U) = \begin{cases} 1 & \text{if } f \text{ rotational harmonic} \\ 0 & \text{if } f \text{ not rotational harmonic} \end{cases} \quad (2)$$

The pattern that results from filtering the difference pattern with the above filter will be referred to as *reduced pattern* in the following, and mathematically is given by the following equation:

$$\rho(U) = p(U) * h(U) \quad (3)$$

An example of the above procedure is given in Fig. 1. In Fig. 1(a) we can see the power spectrum of unsteady pressure transducer 2 in the frequency band 0-6500 Hz, for the healthy case, while Fig. 1(b) shows the corresponding power spectrum for Fault 4. The difference pattern and the reduced pattern are shown in Figs. 1(c) and 1(d), respectively.

It is now evident that reduced pattern consists of a set of values $\rho_i(U)$, corresponding to frequencies (that are multiples of the shaft rotational frequency f). In the following discussion, we will refer to $\rho_i(U)$ as $p_i(U)$, where $p_i(U)$ is the reduced pattern at frequency i/f . If we consider an N -dimensional space with coordinates the N shaft harmonics in the considered frequency band, a reduced pattern corresponds to one point in this space (the point is defined by the values of the coordinates, which are the N values contained in $p_i(U)$).

Before introducing the discriminants derived from the reduced index patterns, we should mention the necessary features of reduced patterns that make them suitable for fault classification. This index is defined by the values of the coordinates, which are the N values contained in $p_i(U)$.

A first indication of the differentiation of the readings of a specific instrument by a fault is the amplitude of the corresponding reduced pattern (the "amplitude" we mean the range between the minimum and maximum values of the pattern). If the reduced pattern of a fault is of higher amplitude than that of another fault, this means that the transducer is more sensitive to the first fault than to the second.

On the other hand, in order to be suitable as fault signatures, the reduced patterns have to exhibit two basic features: (a) Reduced patterns corresponding to one fault should be similar, when different experiments with this fault are considered.

(b) Reduced patterns of two different faults should be dissimilar in order to be distinguishable.

For the practical purpose of classifying patterns according to their corresponding faults, it is required that a higher degree of similarity exist between patterns of one fault, than exists between patterns of different faults.

In order to apply similarity criteria, which are objective (do not depend on the opinion of the experimenter), and quantitative (so that a computer can examine them), we introduce scalar similarity discriminants for the patterns, as explained in the following.

3.2 Reduced Pattern Discriminants. Two discriminant functions were selected, one of them expressing the quantitative similarity (influenced by both the shape and amplitude of compared patterns), the other expressing the shape similarity (influenced only by the shape of the compared patterns).

The first discriminant function is the usual Euclidean distance between reduced patterns, when they are viewed as points in an N -dimensional space. It expresses the quantitative similarity between patterns, both in shape and in actual values, and for the reduced patterns P_1 and P_2 is defined by the following equations:

$$d_1(P_1, P_2) = \frac{1}{N} \sum_{i=1}^N (P_1(i) - P_2(i))^2 \quad (5)$$

where $d_1(P_1, P_2)$ = Euclidean distance between the reduced patterns P_1 and P_2 ; $P_1(i)$, $P_2(i)$ = values of the reduced patterns P_1 and P_2 at the i th harmonic of shaft rotational frequency; N = number of rotational harmonics in the considered frequency band.

Small values of this quantity indicate that P_1 and P_2 are similar (identical if $d_1(P_1, P_2) = 0$). It increases for decreasing quantitative similarity between P_1 and P_2 .

The second discriminant function is the normalized cross-correlation coefficient. It expresses the shape similarity between patterns and does not depend on the range of values of the patterns. For the reduced patterns P_1 and P_2 , it is defined by the following equations:

$$d_C(P_1, P_2) = \left| \frac{CC(P_1, P_2)}{AC(P_1) \cdot AC(P_2)} \right| \quad (5)$$

where

$$CC(P_1, P_2) = \frac{1}{N} \sum_{i=1}^N (P_1(i) - \bar{P}_1)(P_2(i) - \bar{P}_2) \quad (5)$$

and

$$AC(P_i) = \left[\frac{1}{N} \sum_{i=1}^N (P_i(i) - \bar{P}_i)^2 \right]^{1/2}, \quad i = 1, 2$$

If one of these two conditions is fulfilled, the considered fault is characterized by an average reduced pattern, which can be distinguished from the other fault patterns. Such an average reduced pattern can be used as a signature of the fault and will be termed a *well-defined pattern* in the following. If the reduced patterns are viewed as points in a multidimensional space, then the concept of a well-defined average reduced pattern can be expressed as the requirement of having all data points from the specific experiment within a super-sphere and all the remaining points outside it. This can be visualized for a two-dimensional space, for example, as shown in Fig. 2. The points of patterns corresponding to the examined fault belong to a circle centered at average pattern, which represents the center of gravity of the points for a well-defined pattern. All the points of the other faults lie outside this circle.

In order to illustrate the application of the above procedure, it has been applied to the data from the experiments described in section 2. Conclusions as to the magnitudes and the representability properties of the four fault patterns are presented and discussed for all the instruments.

4 Measured Signal Features

For each fault and measuring instrument, the averaged reduced pattern is calculated from the data sets at the four operating points described in section 2.

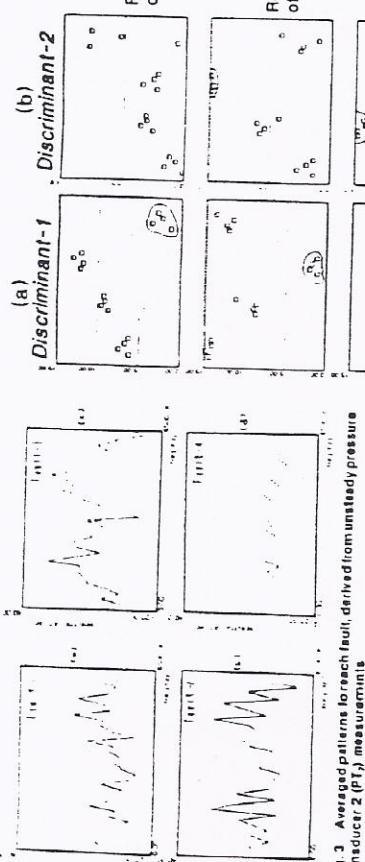


Fig. 3 Averaged patterns for each fault, derived from unsteady pressure transducer 2 (PT2) measurements

4.1 Unsteady Pressure Transducers. The four average-reduced patterns produced by the four faults on PT₂, facing the first stage rotor, are shown in Fig. 3. We remark that Faults 2 and 3 are characterized by high-magnitude patterns. This means that this transducer is highly sensitive to both blading faults of the rotor it faces. On the other hand Fault 1 is characterized by a lower magnitude pattern compared to Faults 2 and 3. So the transducer senses a fault of the rotor one stage downstream, but less intensively. Finally Fault 4 is characterized by a very low magnitude pattern, which means that the transducer is not sensitive to a station fault of the same stage. This is probably due to the fact that Fault 4 is not rotating and its location although very near to the transducer axially is circumferentially 90 deg apart from it.

The values of the discriminants calculated for each reference pattern and all the other reduced patterns are shown in Fig. 4. In Fig. 4(a) we see the values of the Euclidean distance between the average patterns of Fault 1 on one hand and the four patterns of this fault, as well as the twelve other fault patterns on the other. The first four patterns, corresponding to Fault 1 at operating points A, B, C, D are characterized by lower Euclidean distance values than all the other patterns. Therefore Fault 1 has a well-defined pattern on the signals of PT₂, using the Euclidean distance. We can see that the same happens with the other three faults as well.

In Fig. 4(b) the values of the normalized cross-correlation coefficient between the average pattern of Fault 1 on one hand and the four patterns of this fault and also the twelve other fault patterns on the other. We can remark that the same patterns corresponding to Fault 1 at operating points A, B, C, D are characterized by higher normalized cross-correlation coefficient values than all the other patterns, corresponding to the other three faults. So Fault 1 has a well-defined pattern in ρ_{T_2} , using the normalized cross-correlation coefficient. This is in agreement with what has been concluded using the Euclidean distance. In Fig. 4(b) we can remark that the same happens with faults 2 and 3 but not with Fault 4.

For Fault 4 using the normalized cross-correlation coefficient, the pattern of ρ_{T_2} is found to be not well defined, in disagreement with what has been found using the Euclidean distance. This can be explained taking into account that the patterns of Fault 4 are of low magnitude; therefore they are much more influenced by noise and field changes with the operating point than the other faults patterns. These factors change the shape significantly but the magnitude of the patterns does not change very much. This fact shows that examining the value of one discriminant only may not reveal all the available information.

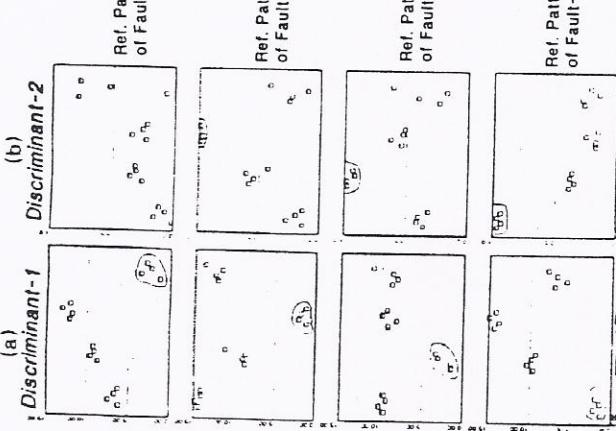


Fig. 4 Discriminant values for data from unsteady pressure transducer 2 (PT2) measurements. All available data sets are compared to each fault reference pattern

Applying the same procedure on the data from transducer ρ_{T_2} gives the results of Fig. 5. We can remark that all faults have well-defined patterns both from the quantitative and the spatial similarity point of view. However, the distances separating the clusters of points corresponding to the data of the various faults are reduced. The discriminability of faults is therefore reduced.

The procedure has been repeated for pressure transducers P_{T_1} and P_{T_3} , leading to the confirmation of the conclusion that the difference patterns, although they are attenuated by traveling downstream some stages, still remain well defined. From the above reduced pattern analysis, we come to the conclusion that blading fault mainly influences the pressure transducer of the corresponding stage, and also influences pressure transducers several stages downstream to a lower degree.

4.2 Accelerometers. As a second step the accelerometers located on the external compressor casing surface were investigated. The average reduced patterns of ACC₁ are shown in Fig. 6. We remark that at ACC₁ Fault 4 is characterized by a high-magnitude pattern, much higher than the same fault at PT₂. The other faults are characterized by lower magnitude patterns. Therefore this accelerometer is very sensitive to Fault 4, but shows also a lower sensitivity to the other three faults. This increased accelerometer sensitivity to Fault 4 is explained if we take into account that Fault 4 is one of stationary blading. The other faults are mechanically connected to the compressor casing, where the accelerometers are located. Discriminant values for the accelerometers are located. Discriminant values for the data from ACC₁ are shown in Fig. 7. We remark that not only Fault 4, but the other faults as well have well-defined patterns both from quantitative and shape similarity point of

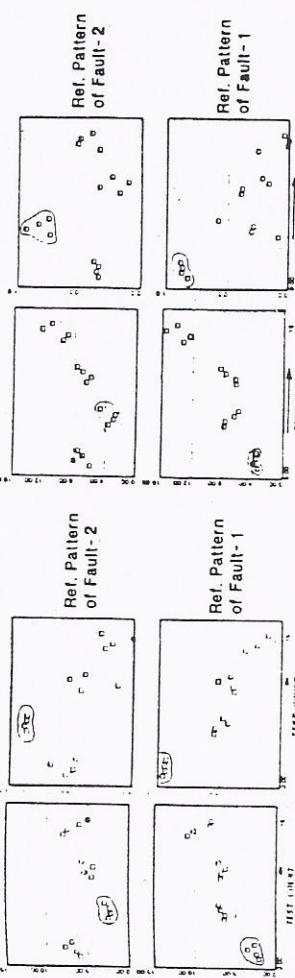
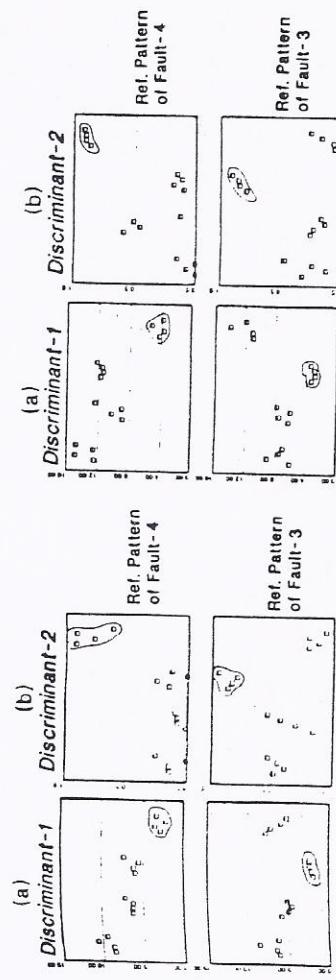


Fig. 3 Averaged patterns for each fault, derived from unsteady pressure transducer 2 (PT2) measurements. All available data sets are compared to each fault reference pattern

them, and Fault 2 presents well-defined patterns in none of the accelerometers.

From the above reduced pattern analysis, we conclude that the accelerometers are all influenced by Faults 3 and 4 significantly. They are also influenced by the other two faults as well, but to a lower extent, depending on the axial and the circumferential position of the accelerometer.

4.3 Microphones. Discriminant values for the data from one of the microphones are shown in Fig. 8. We note that Faults 2, 3, 4 have well-defined patterns, but this does not happen with Fault 1. The conclusion, after repeating the same procedure for the second microphone as well, is that the microphones are influenced significantly by Faults 3 and 4, but also to a lower extent by Faults 1 and 2.

4.4 Bearing Proximity Probes. Discriminant values for the data from bearing proximity probe are shown in Fig. 9.

We remark that only Fault 4 has a well-defined pattern while the others do not. From examining the other bearing proximity probes as well, the conclusion that they show only some sensitivity to Fault 4, while to all the other faults they do not, is confirmed.

5 Automated Fault Diagnosis

Based on the reduced patterns, and the results of the previous section, an automated fault diagnosis method has been developed. This method has as input the time trace of a specific instrument and as output the fault selection based on it. The classification algorithm used, is the minimum-distance

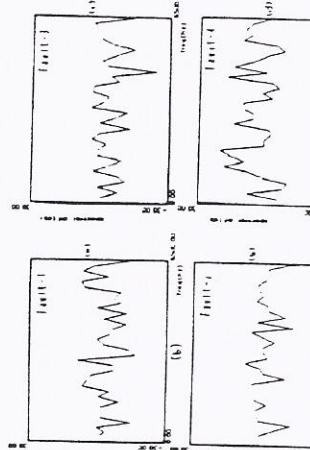


Fig. 5 Discriminant values for data from unsteady pressure transducer 2 (PT2) measurements. All available data sets are compared to each fault reference pattern

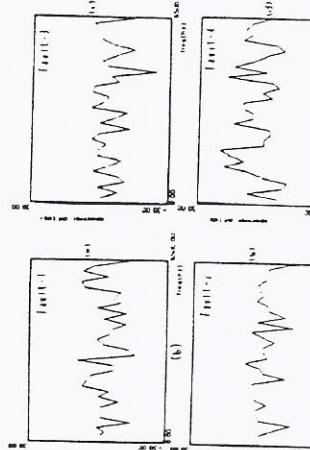


Fig. 6 Averaged patterns for each fault, derived from accelerometer ACC₁ measurements

view. Comparing to the results of Fig. 4, we can also remark that the separation of the clusters is not as clear as for ρ_{T_2} . The same procedure has been repeated for all the accelerometers. It was concluded that at all accelerometers, Fault 4 has a high magnitude pattern, while Fault 3 has only at some of them high magnitude pattern, while in the others lower magnitude ones. Faults 1 and 2 have lower magnitude patterns at all the accelerometers. Also, Faults 3 and 4 have at all the accelerometers well-defined patterns, Fault 1 only at some of

Discriminant-1

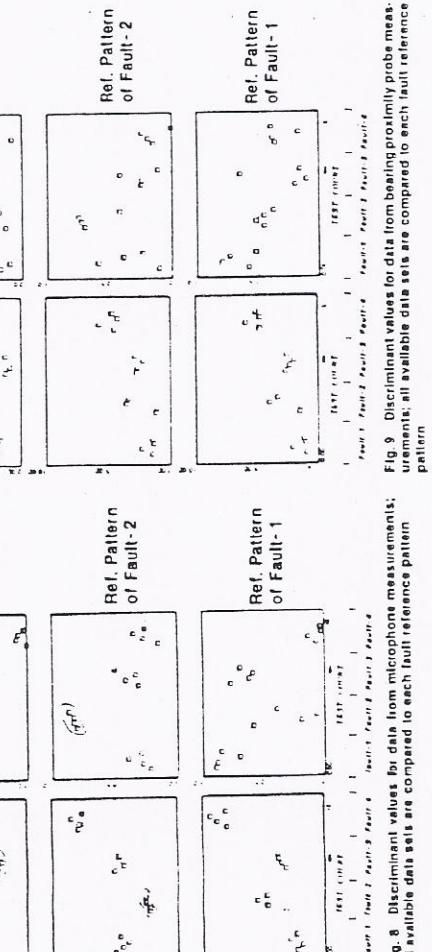
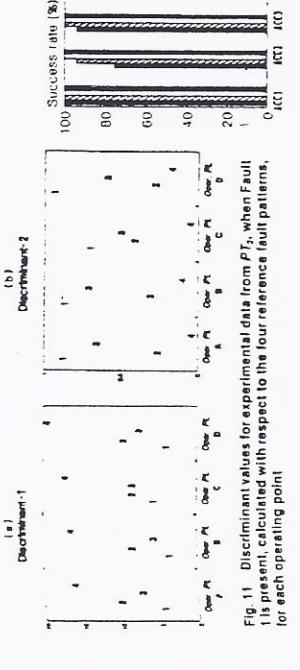


Fig. 8 Discriminant values for data from microphone measurements; all available data sets are compared to each fault reference pattern

method (Sing-Tze, 1984), with number of classes equal to the number of faults.

For the input time trace, first the spectral density and then the reduced difference patterns are calculated. The distances of the calculated reduced pattern from the average reduced pattern of each fault are calculated, and the nearest of the faults is selected. This is given mathematically by the following expression:

For the Euclidean distance

For the correlation coefficient or

For the cross-correlation coefficient or

For the power spectrum or

For the frequency response or

For the insertion loss or

For the selection of the most similar

Fig. 10 Flow chart of the automated fault diagnosis method

Typical results of its application are given for three instruments in Figs. 11–13. In order to demonstrate the principle of the method, Results for P_1^2 signals are given in Fig. 11(a, b) for the Euclidean distance and the normalized cross-correlation coefficient respectively. In Fig. 11(a) we can see the results for the four patterns of Fault 1, corresponding to the operating points A, B, C, D. For each of them we can see the four Euclidean distance values from the four faults' averaged patterns. We remark that for all four patterns the first of the values, corresponding to the average pattern of the first fault, is the lowest. Therefore the above method leads to a correct selection for all four patterns using the Euclidean distance. In Fig. 11(b) we can see the same results as in 11(a), but using the normalized cross-correlation coefficient. Again we remark that for all four patterns the first of the values, corresponding

to the average patterns of the first fault, is the highest. Therefore the above method leads to correct selection, using the normalized cross-correlation coefficient as well.

Corresponding results for the ACC, are shown in Fig. 12, and for the microphone in Fig. 13. We note that for both instruments the above method leads to a correct selection, for the cases of the figures.

The above method has been applied to the experimental data, for all the instruments described in section 2. For each instrument the average reduced patterns of the four faults have been calculated and used as reference patterns. From the results for each instrument the success rates (= percentage of the reduced patterns for which a correct selection has been done)

Discriminant-1

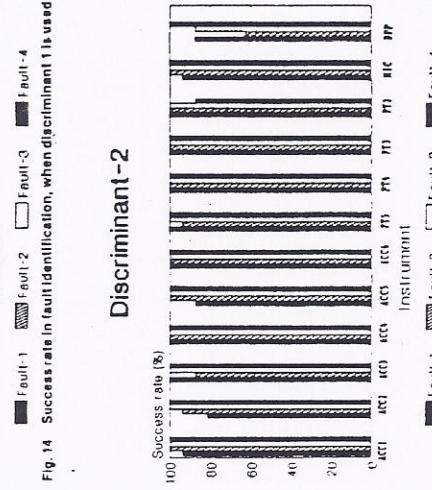
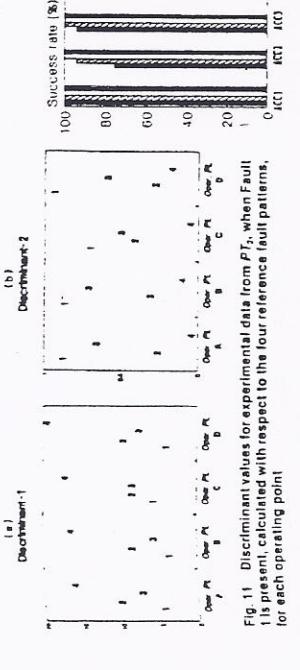


Fig. 11 Discriminant values for experimental data from P_1^2 , when Fault 1 is present, calculated with respect to the four reference (fault patterns, for each operating point)



Fig. 12 Discriminant values for experimental data from ACC, when Fault 1 is present, calculated with respect to the four reference (fault patterns, for each operating point)



Fig. 14 Success rate in fault identification, when discriminant 1 is used

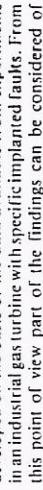


Fig. 15 Success rate in fault identification, when discriminant 2 is used

The technique presented in the previous sections has been developed on the basis of the data available from experiments in an industrial gas turbine with specific implanted faults. From this point of view part of the findings can be considered of general validity while others will be particular to the specific instruments.

6 Discussion

The technique presented in the previous sections has been developed on the basis of the data available from experiments in an industrial gas turbine with specific implanted faults. From this point of view part of the findings can be considered of general validity while others will be particular to the specific engine. The signatures used as a reference for the fault classification came from the experiments. Although they are valid for the particular engine, it is still to be investigated whether they can be used for other engines with the same success. In that respect, it would be very useful if signatures can be produced by computer simulation, in which case a variety of engines would be covered. The research group of the authors has started work in this direction, with some success so far (see Matlioudakis et al., 1991).

On the other hand, in order to extend the present technique to other fault cases, it is necessary to obtain their corresponding signatures. Once such signatures are available, the procedure to be applied is exactly the same. This means that extension to a wider range of faults can be achieved by simply extending the data base of reference fault signatures associated with the technique.

One aspect of the present methodology that might not be of general applicability is the derivation of the reference patterns. Such a pattern should only be tested if new data from independent experiments were added. This statement is also

terns. The application of the filter, which extracts information on shaft rotational harmonics, was based on our observation that blade faults produce differentiation mainly at these harmonics. This means that faults that produce differentiation only of the broad band part of the spectrum or rotor subharmonics (as for example rotating stiction) would not be covered. In that case the part of the technique covering the derivation of the patterns has to be modified by modification of the applied filter Eq. (2). In the same respect, the spectral differences of Eq. (1) can also be replaced by another expression.

A question that arises when monitoring techniques have to be applied is which are the most suitable measurements for this purpose. Although an answer to this question does not emerge from what we have presented, we have tried to include comments on the physical significance of the results obtained. Understanding this significance is helpful in choosing appropriate instruments and measuring locations. An effort to produce a systematic method of investigating this problem is under way.

There are certain aspects of the method that can be improved. For example, the discriminant functions were introduced here on the basis of observations and intuitions. It would be possible to establish such functions from requirement of optimal fulfillment of certain diagnostic criteria. On the other hand, the way that decisions are taken now is of the Yes-No type. It would be desirable to include fault statistics and derive decisions of faults and associated probabilities. Work is under way in these directions by the research group of the authors.

7 Conclusions

A technique for automated fault diagnosis from dynamic measurement data has been developed. Fault patterns were established, by manipulation of signal power spectra. Criteria for examining the suitability of the patterns for fault identification were set. A procedure for examining the possibility to establish reference patterns for each fault and each kind of measurement was presented. Having established such patterns, a technique for deciding whether a

measurement signal corresponds to a particular fault was developed.

The technique was developed on the basis of experimental data coming from various instruments on an industrial gas turbine with implanted blade faults. High rates of success were found on the basis of the available data.

The present technique is such that it can be extended to include a wider range of faults, as long as additional data are available. Finally, suggestions for improving its efficiency were discussed.

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